

**Exercise (2.6.2).** *Note the comments under the listing of the theorem on page 59. Let  $x$  be the limit of the sequence. Add and subtract  $x$  within the absolute value expression.*

**Exercise (2.6.3).** *One of the sequences we discussed in class on Tuesday, 1/22 could be used as the example.*

**Exercise (2.6.4).** *Review the identities in Exercise 1.2.5.*

**Exercise (2.6.5).** *(a) Use the triangle inequality (b) Add and subtract  $x_n y_m$  within the absolute value expression.*

**Exercise (2.6.6).** *(a) Start with an interval  $[a_i, b_i]$  where  $b_i$  is an upper bound for the set, and  $a_i$  is not an upper bound. (b) Let  $I_n = [a_n, b_n]$  and apply the MCT to the sequences  $(a_n)$  and  $(b_n)$ . (c) As in (b) start with a set of nested intervals. This time argue the sequences  $(a_n)$  and  $(b_n)$  are bounded, so that the Bolzano-Weierstrass theorem applies. (d) Use an argument similar to the proof of the Bolzano-Weierstrass theorem, but instead of the NIP, use the fact that the intervals are nested and shrinking to width 0 together with the Cauchy Criterion to establish convergence.*