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In general we can consider a Bernoulli random variable to be the result of an experiment with two outcomes, which for convenience we will label "success" and "failure"

As before we define the Bernoulli random variable X by agreeing to assign the value of 1 to X if the result of the experiment is "success", and zero if the result is "failure":

 $X = \begin{cases} 1 & \text{if the outcome of the experiment is "success"} \\ 0 & \text{if the outcome of the experiment is "failure"} \end{cases}$

Bernoulli Random Variables

To be consistent with the Kolmogorov probability axioms the probability of "success" must be a number p between zero and one (inclusive), and the probability of "failure", which is the compliment of "success", must be 1 - p.

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This results in the following probability mass function f(x) which we will refer to as the *Bernoulli distribution*:

$$f(x) = P(X = x) = \begin{cases} p & \text{if } x = 1\\ 1 - p & \text{if } x = 0 \end{cases}$$

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Most of the discrete probability distributions we will now consider are related to the Bernoulli distribution.

Now consider a series of *independent* experiments, each of which produces a Bernoulli random variable with probability of success p (p is the same for all of the trials)

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If the number of trials n is fixed in advance, the number of successes X has a **binomial** distribution

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If trials continue indefinitely until the first success is obtained, the number of failures obtained X has a **geometric** distribution.

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The following discrete probability distributions arise from this model:

If the number of trials n is fixed in advance, the number of successes X has a **binomial** distribution

If trials continue indefinitely until the first success is obtained, the number of failures obtained X has a **geometric** distribution.

If trials continue indefinitely until the r^{th} success is obtained, the number of failures obtained X has a **negative binomial** distribution.

Note that the geometric distribution is a special case of the negative binomial distribution, with r = 1.

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However, the characterization as a sequence of Bernoulli trials that ends at the r^{th} success is common to all definitions.

That said, you should be prepared to encounter a different definition of X (and a different, but equivalent pmf)if you look at a different text.

The other related distribution we will consider is the **Poisson** distribution.

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The Poisson is a limiting form of the binomial distribution that you get if you let *n* become very large and the probability of success *p* very small, but always keep $np = \lambda$ the same.

Another way to say this is that we take binomial random variables with larger and larger n, but we keep the *expected* number of successes $np = \lambda$ the same for all of them.

The limit of the distribution of such a sequence of random variables as $n \to \infty$ is a Poisson.

The binomial experiment consists of:

- *n* independent Bernoulli trials are performed
- The random variable X is the sum of the results (i.e., the number of successes)
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The probability mass function (pmf) f(x) is:

$$f(x) = P(X = x) = b(x; n, p) = \binom{n}{x} p^x (1-p)^{n-x}, \quad x = 0, 1, 2, \dots$$

It is not obvious, but if you sum the values of f(x) over all values from zero to n, the sum is one.

$$\sum_{x=0}^{n} \binom{n}{x} p^x (1-p)^{n-x} = 1$$

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One way to make this clear is to consider the algebraic identity

$$(x+y)^n = \sum_{i=0}^n \binom{n}{i} x^i y^{n-i}$$

If we let x be the probability of success p and y the probability of failure 1 - p, on substitution we get

$$[p + (1 - p)]^n = 1^n = 1 = \sum_{x=0}^n \binom{n}{x} p^x (1 - p)^{n-x} \quad 0 \le p \le 1$$

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For any distribution, the cumulative distribution function (cdf) F(x), is always defined by

$$F(x) = P(X \le x)$$

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For the binomial distribution, this gives:

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Values of F(x) for the binomial can be obtained from:

- Tables (See table A.1 in the appendix)
- Spreadsheets: = BINOMDIST(x, n, p, TRUE)
- **R**: pbinom(x, n, p)

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Example: A fair coin is tossed 10 times. What is the probability that 7 or fewer heads turn up?

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- **•** R : pbinom(x, n, p)

Example: A fair coin is tossed 10 times. What is the probability that 7 or fewer heads turn up?

We want $P(X \le 7)$, the probability that a binomial experiment with 10 trials and probability of success 0.5 produces 7 or fewer "successes".

If you are using a spreadsheet, enter:

= BINOMDIST(7, 10, 0.5, TRUE)

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If you are using Table A.1, look under n = 10 on page 664, in the row with x = 7 and column with p = 0.50

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All of these should give the value F(7) = .945

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This means that if we toss a fair coin 10 times, the probability of 7 or fewer heads is .945

If we repeat the experiment, tossing the coin 10 times, over and over, the *proportion* of all of the replications of the experiment that have 7 or fewer heads will approach .945.
Example: Suppose every time the Red Sox play the Yankees, the probability that the Red Sox win is 0.6.

If they play 7 games, what is the probability that the Red Sox win 5 or fewer?

Example: Suppose every time the Red Sox play the Yankees, the probability that the Red Sox win is 0.6.

If they play 7 games, what is the probability that the Red Sox win 5 or fewer?

If we assume that each game is an independent Bernoulli trial with probability of "success" equal to 0.6, then the number of games the Red Sox win will have a binomial distribution with n = 7 and p = 0.6.

We want to find the probability that the Red Sox win 5 or fewer,

 $P(X \le 5) = F(5)$

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In R, enter *pdist(5,7,0.6)*

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 $P(X \le 5) = F(5)$

Since there is no simple formula for F for a binomial distribution, we have to use one of the methods listed earlier

In R, enter *pdist(5,7,0.6)*

The result should be 0.841

Example: A baseball player has a .300 batting average.

If the player gets to bat five times in a game, what is the probability that he gets one hit or less:

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If the player gets to bat five times in a game, what is the probability that he gets one hit or less:

We'll assume a binomial distribution with n = 5 and p = 0.300, then we want $F(1) = P(X \le 1)$:

In R enter: *pdist(1,5,0.300)*

Example: A baseball player has a .300 batting average.

If the player gets to bat five times in a game, what is the probability that he gets one hit or less:

We'll assume a binomial distribution with n = 5 and p = 0.300, then we want $F(1) = P(X \le 1)$:

In R enter: *pdist(1,5,0.300)*

The result is 0.528, so in games where a .300 hitter bats five times, more than 50 percent of the time they get one hit or less.

Example: The probability that it rains on a given weekend is 0.20.

In a month with four weekends, what is the probability that two or fewer are rainy?

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In a month with four weekends, what is the probability that two or fewer are rainy?

Assume a binomial distribution with n = 4 and p = 0.2.

In R enter: *pdist(2,4,0.20)*

Example: The probability that it rains on a given weekend is 0.20.

In a month with four weekends, what is the probability that two or fewer are rainy?

Assume a binomial distribution with n = 4 and p = 0.2.

In R enter: *pdist(2,4,0.20)*

The result is 0.9728,

Example: If

$$F(x) = P(X \le x)$$

is the probability of the event A="x or fewer successes", the **compliment** of this event A' is "more than x successes"

Recall that the probability of the compliment A' is always 1 - P(A).

If the chance of rain on a weekend is 0.2 and there are four weekends in a month, what is the probability that it rains on more than 2 weekends?

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In R enter: *1-pdist(2,4,0.20)*

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In R enter: 1-pdist(2,4,0.20)

The result is 0.0272,

The expected value of a binomial random variable E(X) is:

$$E(X) = \sum_{x=0}^{n} x \cdot f(x)$$

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To find the variance V(X) of a binomial random variable, first we find $E(X^2)$:

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Then

and

$$V(X) = E(X^{2}) - [E(X)]^{2} = n^{2}p^{2} - np^{2} + np - n^{2}p^{2}$$

$$V(X) = np(1-p)$$

Now we will perform some numerical experiments. First generate a sample of 1,000,000 observations for a binomial experiment with n = 6 trials and probability of success p = 0.4:

x<*-rbinom*(1000000,6,0.4)

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Now plot a histogram of the results: *hist(x)*

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x<*-rbinom*(1000000,6,0.4)

Now plot a histogram of the results: *hist(x)*

To get a table of the results enter table(x)

The results should look something like:

012345776472588413466232302757625310361

0 1 2 3 4 5 77647 258841 346623 230275 76253 10361 Now compare the frequencies to the probabilities. First compute the probability that X = 0: *dbinom(0,5,0.4)*

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The result should be something like [1] 0.07776

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The result should be something like

[1] 0.07776

To get the probability that X = 1 enter *dbinom(1,5,0.4)*

0 1 2 3 4 5 77647 258841 346623 230275 76253 10361 Now compare the frequencies to the probabilities. First compute the probability that X = 0: dbinom(0,5,0.4)

The result should be something like

[1] 0.07776

To get the probability that X = 1 enter *dbinom(1,5,0.4)*

This time the results should look something like:

[1] 0.2592

0 1 2 3 4 5 77647 258841 346623 230275 76253 10361 Next compute the probability that X = 2: dbinom(2,5,0.4)

0 1 2 3 4 5 77647 258841 346623 230275 76253 10361 Next compute the probability that X = 2: dbinom(2,5,0.4)

The result should be something like

[1] 0.3456

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The result should be something like

[1] 0.3456

To get the probability that X = 5 enter *dbinom(1,5,0.4)*

0 1 2 3 4 5 77647 258841 346623 230275 76253 10361 Next compute the probability that X = 2: *dbinom(2,5,0.4)* The result should be something like

[1] 0.3456

To get the probability that X = 5 enter *dbinom(1,5,0.4)*

This time the results should look something like: [1] 0.01024

The expected value E(X) in this case is:

$$E(X) = np = 5 \cdot 0.4 = 2$$

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To compute the sample mean \overline{x} , enter *mean(x)*

The expected value E(X) in this case is:

$$E(X) = np = 5 \cdot 0.4 = 2$$

To compute the sample mean \overline{x} , enter *mean(x)* The result should be something like [1] 1.999759

The variance V(X) in this case is:

$$V(X) = np(1-p) = 5 \cdot 0.4 \cdot 0.6 = 1.2$$
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To compute the sample variance s^2 , enter *var(x)*

The variance V(X) in this case is:

$$V(X) = np(1-p) = 5 \cdot 0.4 \cdot 0.6 = 1.2$$

To compute the sample variance s^2 , enter *var(x)* The result should be something like [1] 1.197966

At a certain intersection, the probability that a car goes stright through is 0.8.

If we observe 15 cars, what is the probability that 10 or fewer go straight through?

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Enter *pbinom(10,15,0.8)*

At a certain intersection, the probability that a car goes stright through is 0.8.

If we observe 15 cars, what is the probability that 10 or fewer go straight through?

Enter *pbinom(10,15,0.8)* The result should be .164

92% of a certain airline's flights arrive on time.

On a day when the airline operates 30 flights, what is the probablility that more than 27 arrive on time?

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On a day when the airline operates 30 flights, what is the probablility that more than 27 arrive on time?

Enter 1-pbinom(27,30,0.92)

92% of a certain airline's flights arrive on time.

On a day when the airline operates 30 flights, what is the probablility that more than 27 arrive on time?

Enter 1-pbinom(27,30,0.92) The result should be .565

The geometric experiment consists of:

- Independent Bernoulli trials are performed until the first "success" is obtained
- The random variable X is the number of failures obtained
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The probability mass function (pmf) f(x) is:

$$f(x) = P(X = x) = g(x; p) = p(1 - p)^x, \quad x = 0, 1, 2, 3, \dots$$

If you sum the values of f(x) over all values from zero to infinity, the sum is one.

$$\sum_{x=0}^{\infty} p(1-p)^x = p \cdot \sum_{x=0}^{\infty} (1-p)^n$$

If you sum the values of f(x) over all values from zero to infinity, the sum is one.

$$\sum_{x=0}^{\infty} p(1-p)^x = p \cdot \sum_{x=0}^{\infty} (1-p)^n$$

The sum is now a geometric series with r = 1 - p. The sum of a geometric series is 1/(1 - r), so

$$p \cdot \sum_{x=0}^{\infty} (1-p)^n = p \cdot \left(\frac{1}{1-(1-p)}\right) = p \cdot \frac{1}{p} = 1$$

The expected value of a geometric random variable ${\cal E}({\cal X})$ is:

$$E(X) = \sum_{x=0}^{n} x \cdot f(x)$$

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To find the variance V(X) of a geometric random variable, first we find $E(X^2)$:

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Then

$$V(X) = E(X^{2}) - [E(X)]^{2} = \frac{1-p}{p^{2}}$$

Now we will perform some numerical experiments. First generate a sample of 1,000,000 observations for a geometric experiment with probability of success p = 0.4 at each trial:

x<-*r*geom(1000000,0.4)

Now we will perform some numerical experiments. First generate a sample of 1,000,000 observations for a geometric experiment with probability of success p = 0.4 at each trial:

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Now plot a histogram of the results: *hist(x)*

Now we will perform some numerical experiments. First generate a sample of 1,000,000 observations for a geometric experiment with probability of success p = 0.4 at each trial:

x<*-rgeom*(100000,0.4)

Now plot a histogram of the results: *hist(x)*

To get a table of the results enter *table(x)*

Now we will perform some numerical experiments. First generate a sample of 1,000,000 observations for a geometric experiment with probability of success p = 0.4 at each trial:

x<*-rgeom*(100000,0.4)

Now plot a histogram of the results: *hist(x)*

To get a table of the results enter table(x)

The results through X = 6 should look something like:

012345639942224043114459586377515503100418720

0 1 2 3 4 5 6 399422 240431 144595 86377 51550 31004 18720 Now compare the frequencies to the probabilities. First compute the probability that X = 0: dgeom(0,0.4)

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The result should be something like [1] 0.4

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The result should be something like [1] 0.4

To get the probability that X = 1 enter dgeom(1,0.4)

0 1 2 3 4 5 6 399422 240431 144595 86377 51550 31004 18720 Now compare the frequencies to the probabilities. First compute the probability that X = 0: dgeom(0,0.4)

The result should be something like [1] 0.4

To get the probability that X = 1 enter dgeom(1,0.4)

This time the results should look something like:

```
[1] 0.24
```

0 1 2 3 4 5 6 399422 240431 144595 86377 51550 31004 18720 Next compute the probability that X = 2: dgeom(2,0.4)

0 1 2 3 4 5 6 399422 240431 144595 86377 51550 31004 18720 Next compute the probability that X = 2: dgeom(2,0.4)

The result should be something like

[1] 0.144

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The result should be something like

[1] 0.144

To get the probability that X = 5 enter *dbinom(1,5,0.4)*

0 1 2 3 4 5 6 399422 240431 144595 86377 51550 31004 18720 Next compute the probability that X = 2: dgeom(2,0.4)

The result should be something like

[1] 0.144

To get the probability that X = 5 enter *dbinom(1,5,0.4)*

This time the results should look something like: [1] 0.031104

The expected value E(X) in this case is:

$$E(X) = \frac{1-p}{p} = \frac{.6}{.4} = 1.5$$

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To compute the sample mean \overline{x} , enter mean(x)

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$$E(X) = \frac{1-p}{p} = \frac{.6}{.4} = 1.5$$

To compute the sample mean \overline{x} , enter *mean(x)* The result should be something like [1] 1.499121

The variance V(X) in this case is:

$$V(X) = \frac{1-p}{p^2} = \frac{.6}{.4^2} = 3.75$$

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To compute the sample variance s^2 , enter *var(x)*

The variance V(X) in this case is:

$$V(X) = \frac{1-p}{p^2} = \frac{.6}{.4^2} = 3.75$$

To compute the sample variance s^2 , enter *var(x)* The result should be something like [1] 3.733986