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The real importance of the central limit theorem is that you can almost always treat the sum of a sufficiently large collection of independent random variables as a normal random variable.

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This means you can find the probability that an IQ score or an SAT score falls in a certain range by using the normal distribution.