

Question 1

Suppose $y = f(x)$ is an arbitrary function. The difference quotient

$$\frac{f(a + h) - f(a)}{h}$$

represents:

1. The slope of the tangent line at $x = a$
2. The instantaneous rate of change of f at $x = a$
3. The slope of the secant from $(a, f(a))$ to $(a + h, f(a + h))$
4. The average rate of change of f from a to $a + h$
5. 1. and 2.
6. 3. and 4.

Question 1

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5. 1. and 2.
6. 3. and 4.
6. (3 and 4 both)

Question 2

Suppose $y = f(x)$ is an arbitrary function. If it exists, the limit

$$\lim_{h \rightarrow 0} \frac{f(a+h) - f(a)}{h}$$

represents:

1. The slope of the tangent line at $x = a$
2. The instantaneous rate of change of f at $x = a$
3. The slope of the secant from $(a, f(a))$ to $(a+h, f(a+h))$
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5. 1. and 2.
6. 3. and 4.
5. (1 and 2 both)

Question 3

Suppose f is differentiable at $x = a$. Then $f'(a)$ represents:

1. The slope of the tangent line at $x = a$
2. The instantaneous rate of change of f at $x = a$
3. The slope of the secant from $(a, f(a))$ to $(a + h, f(a + h))$
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5. 1. and 2.
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Question 3

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 5. 1. and 2.
 6. 3. and 4.
-
5. (1 and 2 both)

Question 4

Suppose $y = f(t)$ represents the position of a particle at time t . The difference quotient

$$\frac{f(t + h) - f(t)}{h}$$

represents:

1. The instantaneous velocity at time t
2. The average velocity from time t to $t + h$
3. The instantaneous velocity at time $t + h$
4. The instantaneous acceleration at time t
5. The average acceleration from time t to $t + h$
6. The position at time $t + h$

Question 4

Suppose $y = f(t)$ represents the position of a particle at time t . The difference quotient

$$\frac{f(t + h) - f(t)}{h}$$

represents:

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 2. The average velocity from time t to $t + h$
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 5. The average acceleration from time t to $t + h$
 6. The position at time $t + h$
- 2.
-

Question 5

Suppose $y = f(t)$ represents the position of a particle at time t . If it exists, the limit

$$\lim_{h \rightarrow 0} \frac{f(t+h) - f(t)}{h}$$

represents:

1. The instantaneous velocity at time t
2. The average velocity from time t to $t+h$
3. The instantaneous velocity at time $t+h$
4. The instantaneous acceleration at time t
5. The average acceleration from time t to $t+h$
6. The position at time $t+h$

Question 5

Suppose $y = f(t)$ represents the position of a particle at time t . If it exists, the limit

$$\lim_{h \rightarrow 0} \frac{f(t+h) - f(t)}{h}$$

represents:

1. The instantaneous velocity at time t
 2. The average velocity from time t to $t+h$
 3. The instantaneous velocity at time $t+h$
 4. The instantaneous acceleration at time t
 5. The average acceleration from time t to $t+h$
 6. The position at time $t+h$
- 1.
-

Question 6

Suppose $y = f(t)$ is differentiable and represents the position of a particle at time t . If it exists, the limit

$$\lim_{h \rightarrow 0} \frac{f'(t+h) - f'(t)}{h}$$

represents:

1. The instantaneous velocity at time t
2. The average velocity from time t to $t+h$
3. The instantaneous velocity at time $t+h$
4. The instantaneous acceleration at time t
5. The average acceleration from time t to $t+h$
6. The position at time $t+h$

Question 6

Suppose $y = f(t)$ is differentiable and represents the position of a particle at time t . If it exists, the limit

$$\lim_{h \rightarrow 0} \frac{f'(t+h) - f'(t)}{h}$$

represents:

1. The instantaneous velocity at time t
 2. The average velocity from time t to $t+h$
 3. The instantaneous velocity at time $t+h$
 4. The instantaneous acceleration at time t
 5. The average acceleration from time t to $t+h$
 6. The position at time $t+h$
- 4.
-

Question 7

Suppose $f(x)$ is a function. Which of the following are true?

1. f can be differentiable but not continuous at $x = a$
2. f can be continuous but not differentiable at $x = a$
3. If f is continuous at $x = a$, it is differentiable there
4. If f is differentiable at $x = a$, it is continuous there
5. (both 1 and 3)
6. (both 2 and 4)

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Question 8

Suppose $f(x)$ is a function defined for all real numbers and $a < b$. To apply the Intermediate Value Theorem on the interval from a to b , it must be true that:

1. f is continuous on (a, b)
2. f is continuous on $[a, b]$
3. $f(a) = f(b)$
4. $f(a) \neq f(b)$
5. (both 1 and 3)
6. (both 2 and 4)

Question 8

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5. (both 1 and 3)
6. (both 2 and 4)
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Question 9

Suppose $f(x)$, $g(x)$, and $h(x)$ are functions and

$$f(x) \leq g(x) \leq h(x) \quad \text{for all } x$$

To determine $\lim_{x \rightarrow a} g(x)$ using the squeeze theorem, it must be true that:

1. $\lim_{x \rightarrow a} f(x)$ exists
2. $\lim_{x \rightarrow a} g(x)$ exists
3. $\lim_{x \rightarrow a} h(x)$ exists
4. $\lim_{x \rightarrow a} f(x) = \lim_{x \rightarrow a} h(x)$
5. All of the above
6. (1,3, and 4 only)

Question 9

Suppose $f(x)$, $g(x)$, and $h(x)$ are functions and

$$f(x) \leq g(x) \leq h(x) \quad \text{for all } x$$

To determine $\lim_{x \rightarrow a} g(x)$ using the squeeze theorem, it must be true that:

1. $\lim_{x \rightarrow a} f(x)$ exists
2. $\lim_{x \rightarrow a} g(x)$ exists
3. $\lim_{x \rightarrow a} h(x)$ exists
4. $\lim_{x \rightarrow a} f(x) = \lim_{x \rightarrow a} h(x)$
5. All of the above
6. (1,3, and 4 only)
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Question 10

Suppose $f(x)$ is defined piecewise by

$$f(x) = \begin{cases} |x - 1| & \text{if } x < 0 \\ ab^x & \text{if } x \geq 0 \end{cases} \quad b > 0$$

What value of a makes f continuous at $x = 0$?

1. $a = 0$
2. $a = -1$
3. $a = 1$
4. $a = 2$
5. Cannot be determined
6. None of the above

Question 10

Suppose $f(x)$ is defined piecewise by

$$f(x) = \begin{cases} |x - 1| & \text{if } x < 0 \\ ab^x & \text{if } x \geq 0 \end{cases} \quad b > 0$$

What value of a makes f continuous at $x = 0$?

1. $a = 0$
 2. $a = -1$
 3. $a = 1$
 4. $a = 2$
 5. Cannot be determined
 6. None of the above
3. $a = 1$

Question 11

Find the derivative of

$$f(x) = \frac{1}{x}$$

directly from the definition as a limit of a difference quotient.

1. $-1/x$

2. $1/x$

3. $\ln x$

4. $-1/x^2$

5. $1/x^2$

6. none of the above

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3. $\ln x$

4. $-1/x^2$

5. $1/x^2$

6. none of the above

4.

Question 12

A particle moves along a straight line with its position at time t given by the function

$$f(t) = 10 + 50t - 12t^2$$

Find a formula for the **average velocity** from $t = 0$ to $t = a$.

- | | |
|------------------|----------------------|
| 1. $50 - 12a^2$ | 4. $50 + 12a$ |
| 2. $50a - 12$ | 5. $50 + 12a^2$ |
| 3. $50a - 12a^2$ | 6. none of the above |

Question 12

A particle moves along a straight line with its position at time t given by the function

$$f(t) = 10 + 50t - 12t^2$$

Find a formula for the **average velocity** from $t = 0$ to $t = a$.

- | | |
|------------------|----------------------|
| 1. $50 - 12a^2$ | 4. $50 + 12a$ |
| 2. $50a - 12$ | 5. $50 + 12a^2$ |
| 3. $50a - 12a^2$ | 6. none of the above |

6. The average velocity from $t = 0$ to $t = a$ is $50 - 12a$

Question 13

A particle moves along a straight line with its position at time t given by the function

$$f(t) = 10 + 50t - 12t^2$$

Find a formula for the **instantaneous velocity** at $t = a$.

- | | |
|-----------------|----------------------|
| 1. $50 - 12a$ | 4. $50 - 24a^2$ |
| 2. $50 - 24a$ | 5. $50 + 12a^2$ |
| 3. $50 - 12a^2$ | 6. none of the above |

Question 13

A particle moves along a straight line with its position at time t given by the function

$$f(t) = 10 + 50t - 12t^2$$

Find a formula for the **instantaneous velocity** at $t = a$.

- | | | | |
|----|--------------|----|-------------------|
| 1. | $50 - 12a$ | 4. | $50 - 24a^2$ |
| 2. | $50 - 24a$ | 5. | $50 + 12a^2$ |
| 3. | $50 - 12a^2$ | 6. | none of the above |

2.

Question 14

A particle moves along a straight line with its position at time t given by the function

$$f(t) = 10 + 50t - 12t^2$$

Find a formula for the **instantaneous acceleration** at $t = a$.

- | | |
|-------------|----------------------|
| 1. $-12a$ | 4. $24a$ |
| 2. $-24a$ | 5. -24 |
| 3. $-12a^2$ | 6. none of the above |

Question 14

A particle moves along a straight line with its position at time t given by the function

$$f(t) = 10 + 50t - 12t^2$$

Find a formula for the **instantaneous acceleration** at $t = a$.

- | | |
|-------------|----------------------|
| 1. $-12a$ | 4. $24a$ |
| 2. $-24a$ | 5. -24 |
| 3. $-12a^2$ | 6. none of the above |
- 5.

Question 15

Suppose

$$\frac{x - \sqrt{2}}{x^2 - 2} \leq g(x) \leq \frac{x^2 - 4}{x - 2}$$

If possible, use the squeeze theorem to find the limit of $g(x)$ as $x \rightarrow 2$.

- | | | | |
|----|------|----|----------------------|
| 1. | 2 | 4. | 1/4 |
| 2. | -2 | 5. | 1/2 |
| 3. | -1/2 | 6. | cannot be determined |

Question 15

Suppose

$$\frac{x - \sqrt{2}}{x^2 - 2} \leq g(x) \leq \frac{x^2 - 4}{x - 2}$$

If possible, use the squeeze theorem to find the limit of $g(x)$ as $x \rightarrow 2$.

1. 2

4. $1/4$

2. -2

5. $1/2$

3. $-1/2$

6. cannot be determined

6.

Question 16

Suppose $f(x) = 3 + x$ and $g(x) = 3x^2$, can we use the Intermediate Value Theorem to show that

$$f(x) - g(x)$$

has a root in the interval $[0, 1]$?

1. Yes
2. No, because $(f - g)(x)$ is not continuous on $[0, 1]$
3. No, because $(f - g)(0) = (f - g)(1)$
4. No, because 0 is not between $(f - g)(0)$ and $(f - g)(1)$

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 4. No, because 0 is not between $(f - g)(0)$ and $(f - g)(1)$
- 4.

Question 17

Suppose

$$f(x) = \begin{cases} \frac{x^2-1}{x-1} & \text{if } x < 2 \\ x^2 & \text{if } x \geq 2 \end{cases}$$

Then f is continuous everywhere except:

- | | |
|---------------|---------------------------------|
| 1. $\{0\}$ | 4. $\{1, 2\}$ |
| 2. $\{1\}$ | 5. $\{0, 2\}$ |
| 3. $\{0, 1\}$ | 6. f is continuous everywhere |

Question 17

Suppose

$$f(x) = \begin{cases} \frac{x^2-1}{x-1} & \text{if } x < 2 \\ x^2 & \text{if } x \geq 2 \end{cases}$$

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| 1. $\{0\}$ | 4. $\{1, 2\}$ |
| 2. $\{1\}$ | 5. $\{0, 2\}$ |
| 3. $\{0, 1\}$ | 6. f is continuous everywhere |

4.

Question 18

Suppose

$$f(x) = \begin{cases} \frac{x^2-1}{x-1} & \text{if } x < 2 \\ x^2 & \text{if } x \geq 2 \end{cases}$$

Is f continuous from the left at $x = 2$?

1. Yes
2. No because $f(2)$ does not exist
3. No because $\lim_{x \rightarrow 2^-} f(x)$ does not exist
4. No because $\lim_{x \rightarrow 2^-} f(x) \neq f(2)$

Question 18

Suppose

$$f(x) = \begin{cases} \frac{x^2-1}{x-1} & \text{if } x < 2 \\ x^2 & \text{if } x \geq 2 \end{cases}$$

Is f continuous from the left at $x = 2$?

1. Yes
2. No because $f(2)$ does not exist
3. No because $\lim_{x \rightarrow 2^-} f(x)$ does not exist
4. No because $\lim_{x \rightarrow 2^-} f(x) \neq f(2)$

4.

Question 19

Suppose

$$f(x) = \begin{cases} \frac{x^2-1}{x-1} & \text{if } x < 2 \\ x^2 & \text{if } x \geq 2 \end{cases}$$

Is f continuous from the right at $x = 2$?

1. Yes
2. No because $f(2)$ does not exist
3. No because $\lim_{x \rightarrow 2^+} f(x)$ does not exist
4. No because $\lim_{x \rightarrow 2^+} f(x) \neq f(2)$

Question 19

Suppose

$$f(x) = \begin{cases} \frac{x^2-1}{x-1} & \text{if } x < 2 \\ x^2 & \text{if } x \geq 2 \end{cases}$$

Is f continuous from the right at $x = 2$?

1. Yes
2. No because $f(2)$ does not exist
3. No because $\lim_{x \rightarrow 2^+} f(x)$ does not exist
4. No because $\lim_{x \rightarrow 2^+} f(x) \neq f(2)$

1.

Question 20

Suppose

$$f(x) = x^2 - 4x - 4$$

Find the equation of the tangent line at $x = 3$

- | | |
|-------------------|----------------------|
| 1. $y = 2x + 13$ | 4. $y = 2x + 7$ |
| 2. $y = -2x + 13$ | 5. $y = 2x - 13$ |
| 3. $y = -2x - 13$ | 6. none of the above |

Question 20

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$$f(x) = x^2 - 4x - 4$$

Find the equation of the tangent line at $x = 3$

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4. $y = 2x + 7$

2. $y = -2x + 13$

5. $y = 2x - 13$

3. $y = -2x - 13$

6. none of the above

5. $y = 2x - 13$